

From Population Growth to Firm Demographics: Implications for Concentration, Entrepreneurship and the Labor Share

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Motivation

- ▶ Puzzling aggregate trends in the US since 1980s
 - ▶ Decline in the **firm entry rate** (14% to 8%)
 - ▶ Decline in **firm exit rate** (9.7% to 7.7%)
 - ▶ Increase in **average firm size** (20 to 24 employees)
 - ▶ Increase in (employment) **concentration** (51% to 58%)
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- ▶ What explains this?
 - ▶ We look at population growth + firm demographics

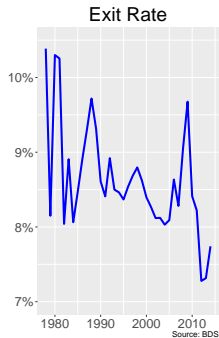
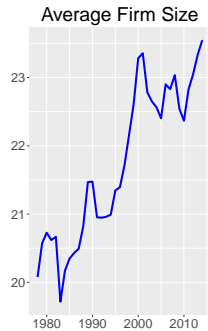
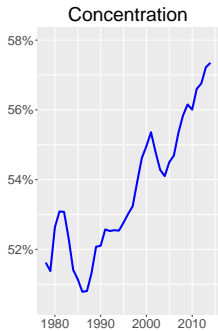
Outline

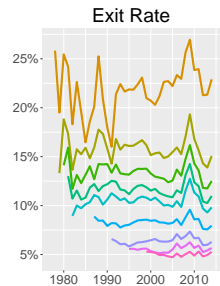
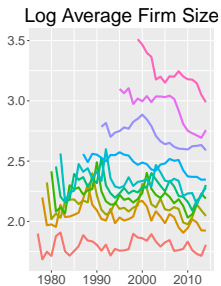
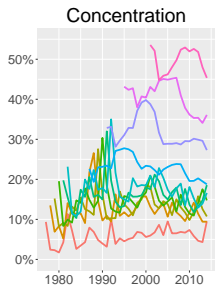
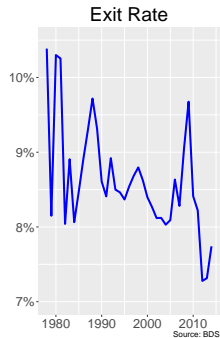
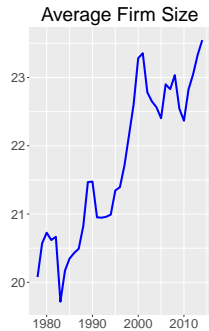
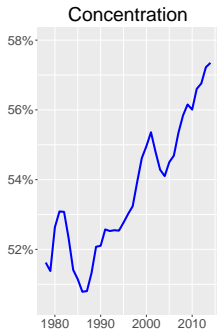
- ▶ Why population growth + firm demographics?
 - ▶ Document new facts
 - ▶ Feedback effects
- ▶ Theory
- ▶ Accounting
- ▶ Calibration
- ▶ Results

Overview of Results

- ▶ Reallocation across firm-age groups accounts for
 - ▶ Concentration
 - ▶ Average firm size
 - ▶ Exit rates
 - ▶ Labor share
- ▶ Declining entry rates generate the reallocation
- ▶ Declining population growth lowers entry rate
- ▶ Feedback from firm demographics to entry is $2/3$ of the effect

Motivating Evidence

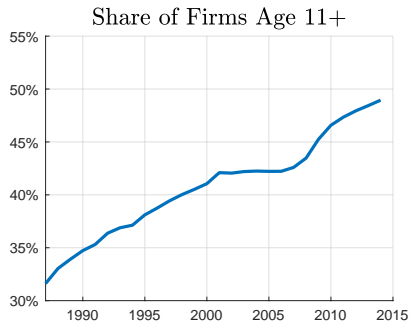




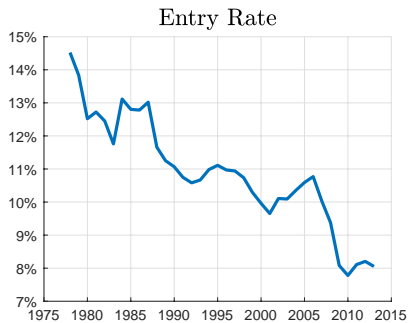
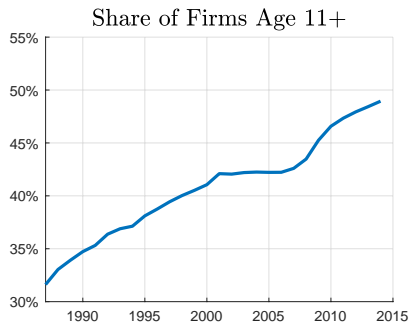
Firm age

- a) 0
- b) 1
- c) 2
- d) 3
- e) 4
- f) 5
- g) 6 to 10
- h) 11 to 15
- i) 16 to 20
- j) 21 to 25

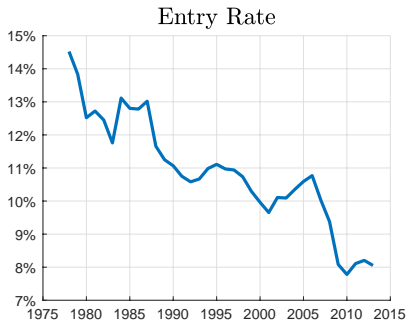
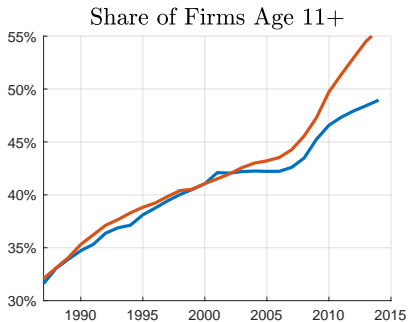
Firms are Aging



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Δ Population Growth \rightarrow Δ Entry Rates

- ▶ Average firm size:

$$e_t \equiv N_t/M_t$$

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$$\hat{M} = \hat{N} - \hat{e} \tag{1}$$

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- ▶ Growth in the number of firms is entry rate minus exit rate

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- ▶ Combining (1) and (2):

$$\lambda = \hat{N} - \hat{e} + \xi$$

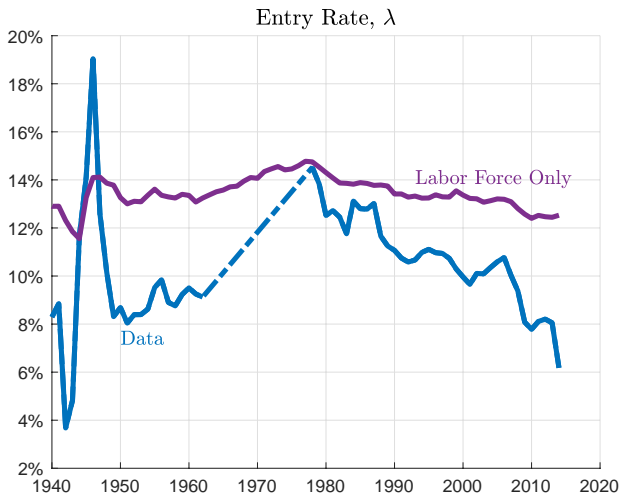
The Rise and Fall of Population Growth



Source: BLS Current Population Survey

Is This Driving Force Enough?

$$\lambda = \hat{N} - \underbrace{\hat{e}}_0 + \underbrace{\xi}_{12\%}$$



Is This Driving Force Enough?

- ▶ Qualitatively yes, quantitatively no.
- ▶ Cannot explain movements in exit rate
- ▶ Cannot explain increase in average size

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- ▶ In the data

$$\underbrace{\Delta\lambda}_{6\%} = \underbrace{\Delta\hat{N}}_{2\%} - \underbrace{\Delta\hat{e}}_{2\%} + \underbrace{\Delta\xi}_{2\%}$$

Firm Demographics

| Age | Average firm size | Exit rate (%) |
|-------|-------------------|---------------|
| 0 | 6.05 | — |
| 1 | 7.73 | 21.85 |
| 2 | 8.46 | 15.86 |
| 3 | 9.14 | 13.43 |
| 4 | 9.77 | 11.68 |
| 5 | 10.36 | 10.48 |
| 6-10 | 11.98 | 8.30 |
| 11-15 | 15.08 | 6.40 |
| 16-20 | 18.81 | 5.56 |
| 21-25 | 24.03 | 4.99 |

Δ Population Growth + Firm Demographics

- ▶ Need to account for firm demographics
- ▶ Important **feedback** effects

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- ▶ Δ entry rates \rightarrow Δ age distribution
- ▶ This affects average firm size
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-
- ▶ Decrease in population growth implies:
 - ▶ Decline in entry rate
 - ▶ Aging of firms

Theory

Environment

- ▶ Common discount factor β
- ▶ Fixed endowment of a resource (labor) N_t inelastically supplied. Numeraire.
- ▶ Firm's idiosyncratic state s
- ▶ $s_t \sim F(s_{t+1}|s_t)$. Persistence.

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- ▶ Accommodates **perfect competition** and **variable markups**

Equilibrium: Definition

An equilibrium for a given sequence $\{N_t\}$ and given initial measure μ_0 are sequences $\{s_t^*, m_t, \mu_t, Z_t\}$

1. **Exit:** Optimal exit condition.
2. **Entry:** No rents for entrants
3. **Resource constraint** holds

Equilibrium: Analysis

- ▶ Guess $Z_t = Z^*$ for all t , where $v^e(Z^*) = 0$

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- ▶ Exit rates, average firm size, and size distributions by cohorts are time invariant.

Resource Constraint

- ▶ Define firm demographic variables:
 - ▶ S_a : Probability an entrant survives at least a periods
 - ▶ e_a : Average size of cohort of age a

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$$N_t = m_t e_0 + E_t^I$$

- ▶ Mass of entrants:

$$m_t = \frac{N_t - E_t^I}{e_0}$$

Dynamic Entry Equation

$$m_t = \frac{N_t - E_t^I}{e_0}$$

- ▶ Employment by incumbents depends on firm demographics

$$E_t^I = \sum_{a=1}^{\infty} m_{t-a} S_a e_a$$

- ▶ History dependence: Current entry depends on past entry

$$m_t = \frac{N_t - \sum_{a=1}^{\infty} m_{t-a} S_a e_a}{e_0}$$

- ▶ Feedback of firm demographics on entry

From Population Growth to Entry

1. Long run effects

- ▶ $\hat{e} = 0$
- ▶ Population growth g affects share of age cohorts:

Lower growth implies lower exit rates

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2. Adjustment Path

- ▶ Change in g implies changes in average size
- ▶ $\hat{e} \neq 0$ in the transition

Accounting

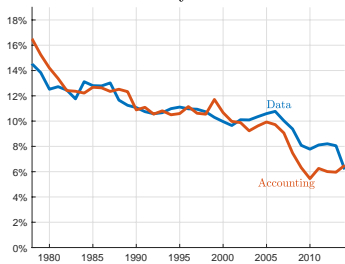
Accounting Exercise

- ▶ Composition effect due to changes in N_t
- ▶ Take firm demographics S_a and e_a from data
- ▶ Feed N_t into dynamic entry equation

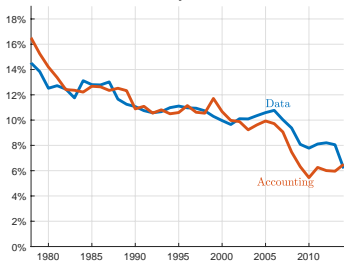
$$m_t = \frac{N_t - \sum_{a=1}^{\infty} m_{t-a} S_a e_a}{e_0}$$

- ▶ Remain agnostic about the underlying model

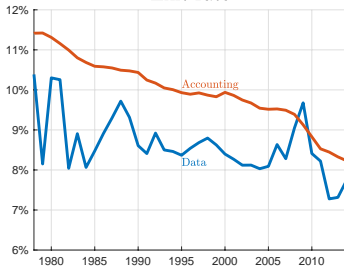
Entry Rate



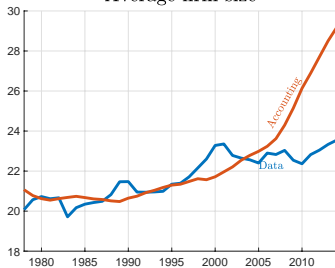
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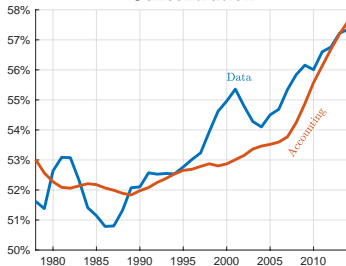
Exit rate



Average firm size



Concentration



▶ Extrapolation necessary due to data limitations ▶ Extrapolation

▶ Do not observe e_a and S_a for older firms (age > 25)

▶ Do not observe μ_0 (age distribution in 1940)

- ▶ Extrapolation necessary due to data limitations ▶ Extrapolation
 - ▶ Do not observe e_a and S_a for older firms (age > 25)
 - ▶ Match time-series of **average firm size** and **exit rates** of left-censored firms ▶ Match
 - ▶ Do not observe μ_0 (age distribution in 1940)
 - ▶ Match time-series of **employment weight** of left-censored firms ▶ Match

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- ▶ Alternative to extrapolation: calibrate a structural model

Calibration

Calibration strategy

- ▶ Pick a model: perfect competition
 - ▶ Homogeneous good
 - ▶ Aggregate state Z equals market price p
- ▶ Assume economy in balanced growth path in 1939
- ▶ Feed labor force growth rate from 1940 to 2014
- ▶ Calibrate to (mostly) 1978 moments
- ▶ Look at non-targeted moments

Functional Forms

- ▶ Production function

$$f(s, n) = sn^\alpha; \quad \alpha < 1$$

- ▶ Log-productivity follows AR(1)

$$\log(s_{t+1}) = \mu_s + \rho \log(s_t) + \varepsilon_{t+1}; \quad \varepsilon_{t+1} \sim \mathcal{N}(0, \sigma_\varepsilon^2)$$

- ▶ Startups draw productivity from

$$G \sim \log \mathcal{N}(s_0, \sigma_0^2)$$

- ▶ Overhead labor is increasing in firm size

$$c_f = c_{fa} + c_{fb} \times h(s)$$

Parameter Values

| Assigned | | | |
|----------|-------|------------------------------|----------|
| | Value | Definition | Basis |
| β | 0.96 | Discount factor | Standard |
| α | 0.64 | Worker's share of output | Standard |
| g | 0.01 | Labor force growth rate (SS) | Standard |

| Jointly Calibrated | | | | | |
|------------------------|---------|--------------------------|------------------------|---------|--------|
| Parameters | | | Moments | | |
| | Value | Definition | | Data | Model |
| c_e | $3e-7$ | Entry cost | $p^* = 1$ | — | — |
| c_{fa} | 3.760 | Operating cost intercept | Avg. firm size 1978 | 20.08 | 20.08 |
| c_{fb} | 0.007 | Operating cost slope | SD log-LP 1993-01 | 0.58 | 0.60 |
| s_0 | -11.189 | Mean of G | Avg. entrant size 1978 | 5.40 | 5.36 |
| σ_0^2 | 3.966 | Variance of G | Avg. conc. of entrants | 5.90% | 5.87% |
| μ_s | -0.025 | Drift in AR(1) | Entry rate 1978 | 14.75% | 14.33% |
| ρ | 0.973 | Persistence of AR(1) | 5-year growth rate | 70.49% | 73.82% |
| σ_ε^2 | 0.073 | Variance of AR(1) shocks | 5-year exit rate | 48.42 % | 45.83% |

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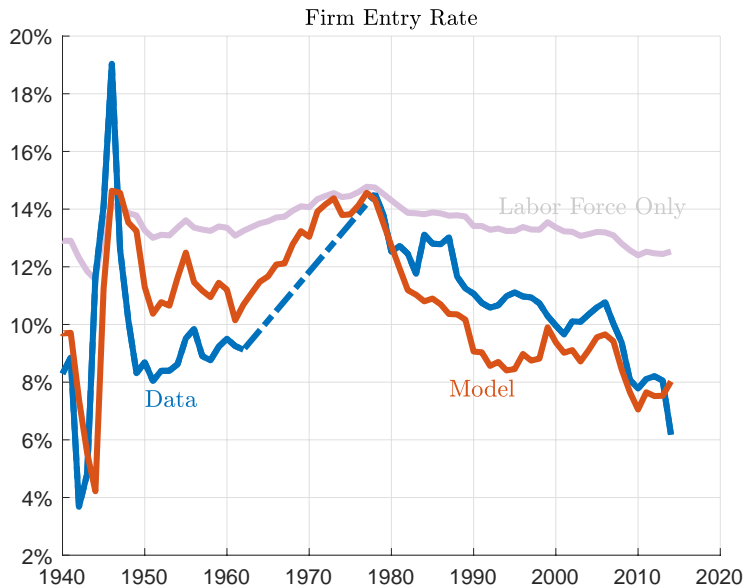
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Non-targeted moments on Firm Dynamics?

Exit, Size, and Concentration by Firm Age

| Age | Exit rate | | Average firm size | | Concentration | |
|-------|-----------|----------|-------------------|-------|---------------|----------|
| | Data(%) | Model(%) | Data | Model | Data(%) | Model(%) |
| 0 | — | — | 6.05 | 5.35 | 5.90 | 5.87 |
| 1 | 21.85 | 29.22 | 7.73 | 6.01 | 12.29 | 7.53 |
| 2 | 15.86 | 18.73 | 8.46 | 6.71 | 13.29 | 9.07 |
| 3 | 13.43 | 14.53 | 9.14 | 7.47 | 14.83 | 10.68 |
| 4 | 11.68 | 12.18 | 9.77 | 8.34 | 16.45 | 12.44 |
| 5 | 10.48 | 10.66 | 10.36 | 9.29 | 17.84 | 14.43 |
| 6-10 | 8.30 | 8.40 | 11.98 | 12.66 | 23.00 | 22.38 |
| 11-15 | 6.40 | 6.47 | 15.08 | 20.52 | 31.85 | 37.62 |
| 16-20 | 5.56 | 5.60 | 18.81 | 30.46 | 40.68 | 50.85 |
| 21-25 | 4.99 | 5.12 | 24.03 | 41.43 | 50.47 | 60.25 |
| 26+ | 4.29 | 4.53 | 81.59 | 72.70 | 78.91 | 73.90 |

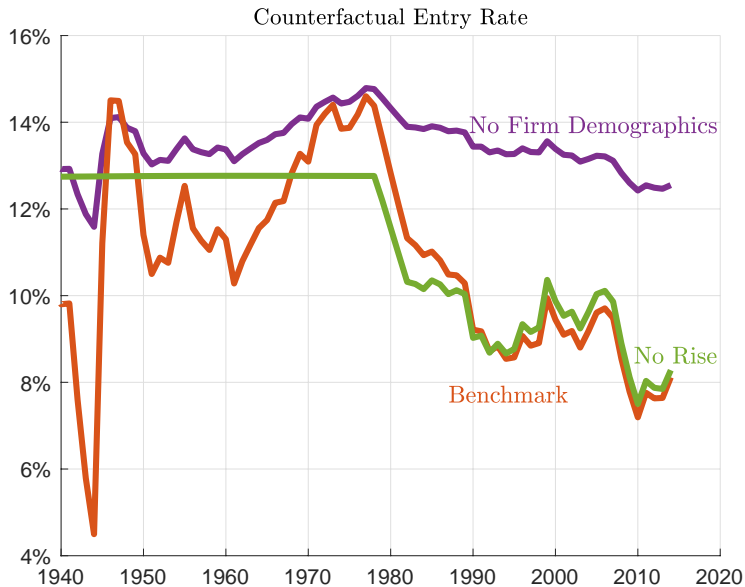
Entry Rate



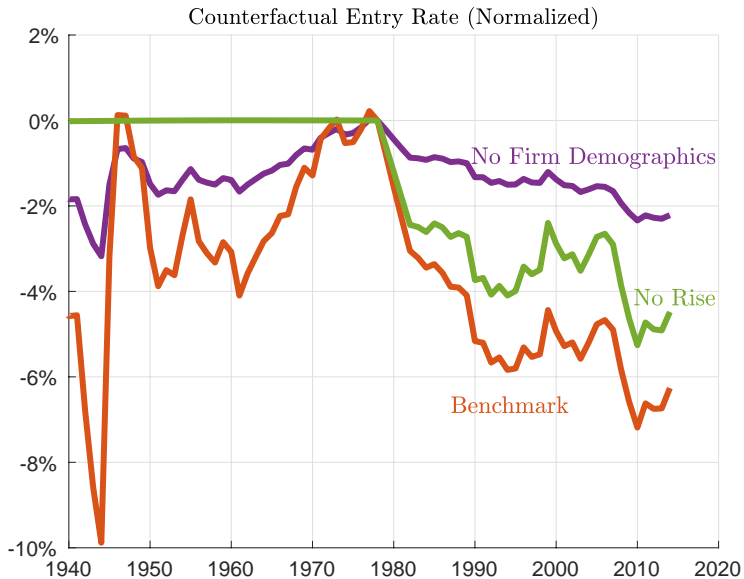
Non-targeted moments



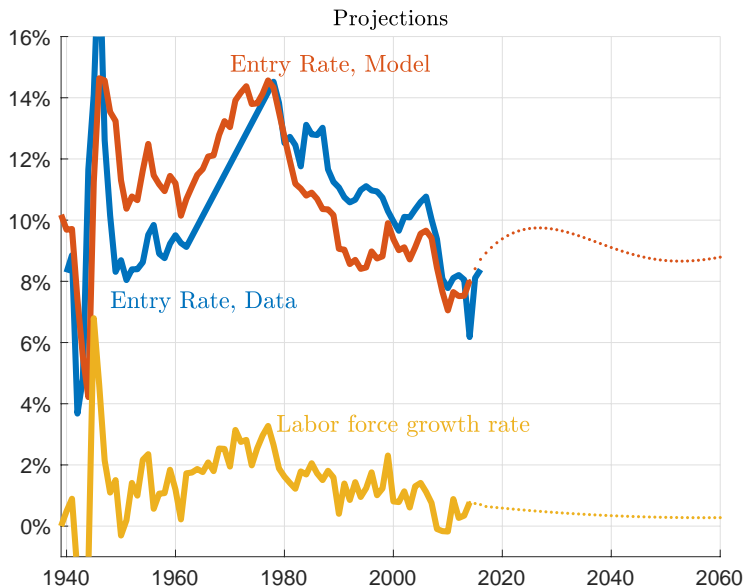
Counterfactuals



Counterfactuals



Projections



Labor share: Autor et al / Kehrig (2019) + Aging

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Labor share: Autor et al / Kehrig (2019) + Aging

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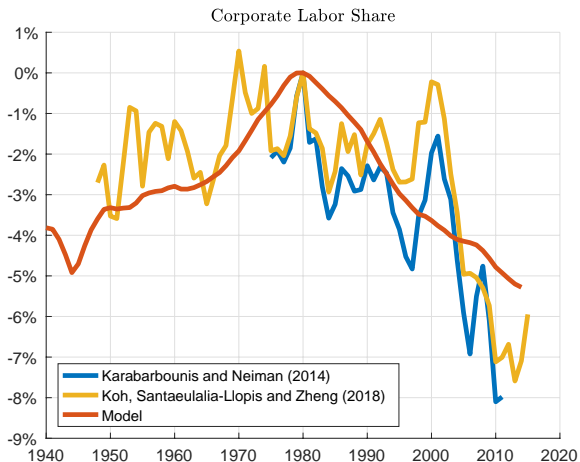
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Discussion

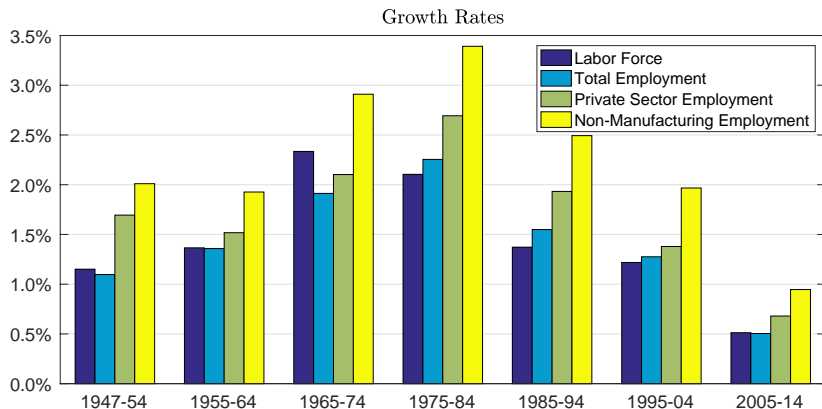
▶ Labor force and labor supply

▶ Job Creation and Destruction

▶ TFP

▶ CONCLUSION

Alternative Measures of Labor Supply



Labor Force Growth Decomposition

▶ Back

$$LF_t = \text{Civilian Noninstitutional Population Age 16 And Over}_t \times \text{Participation Rate}_t$$

Labor Force Growth Decomposition

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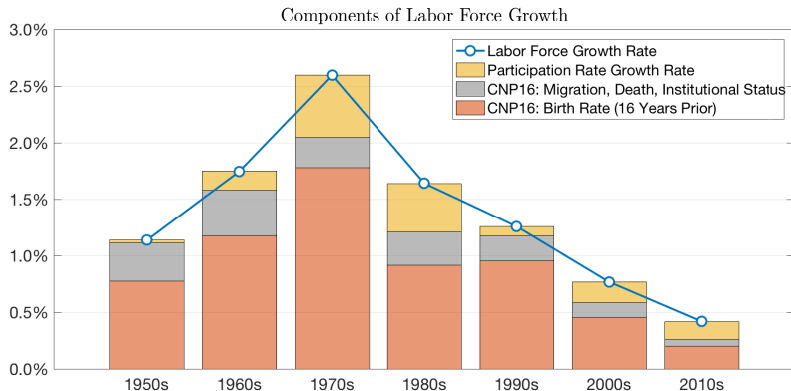
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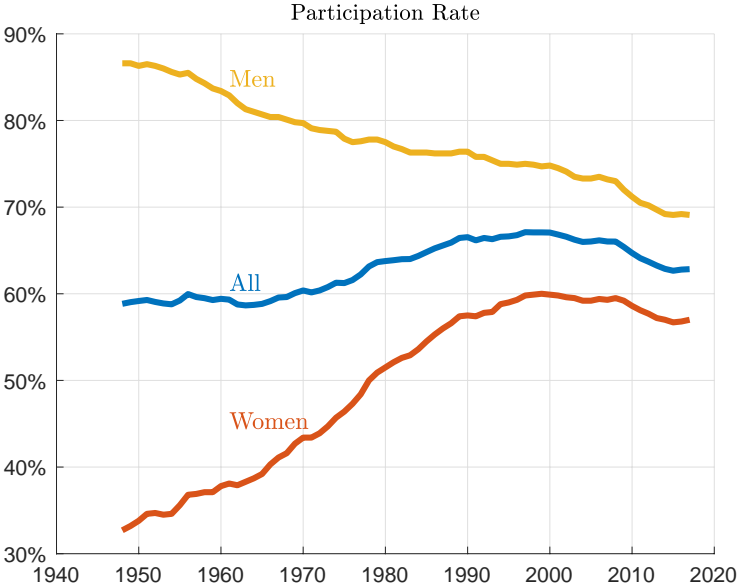
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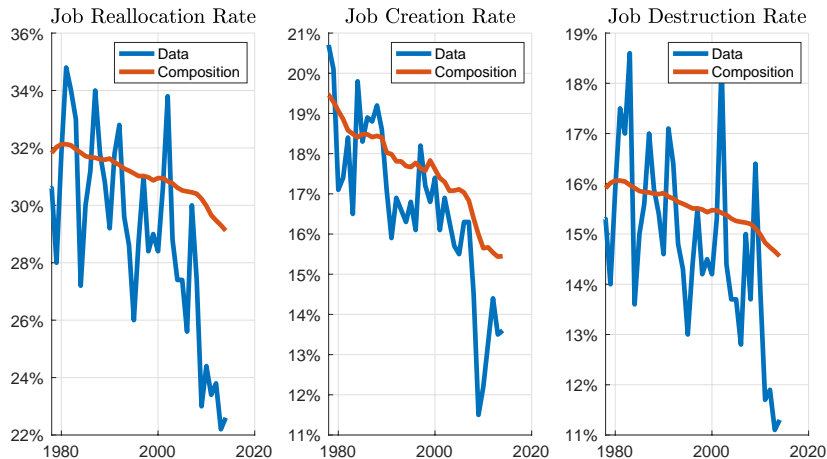
Participation Rate By Gender

[▶ Back](#)



Job Reallocation: Accounting Approach

[▶ Back](#)



TFP Growth by Decade

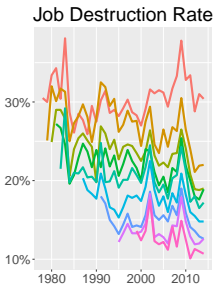
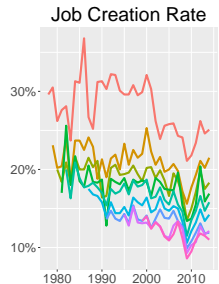
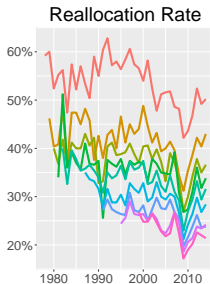
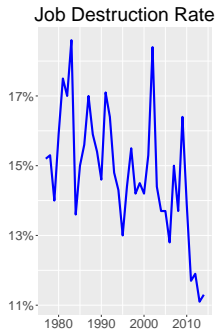
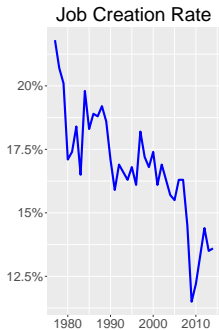
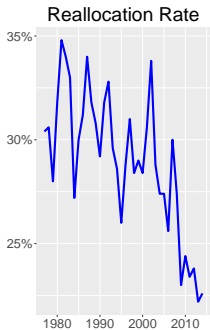
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| | TFP data (%) | Model | |
|-------|--------------|-----------------|--------|
| | | measured TFP(%) | TFP(%) |
| 1950s | 2.35 | 0.43 | -0.16 |
| 1960s | 2.05 | 0.53 | -0.27 |
| 1970s | 1.08 | 0.78 | -0.51 |
| 1980s | 0.51 | 0.79 | 0.46 |
| 1990s | 1.03 | 0.59 | 0.59 |
| 2000s | 0.77 | 0.39 | 0.40 |
| 2010s | 1.11 | 0.23 | 0.47 |

- ▶ Aggregate production function is $Y = AM^{1-\alpha}N^\alpha$.
- ▶ TFP is $A = [\int s^{1/(1-\alpha)} d\mu(s)]^{1-\alpha}$
- ▶ Measured TFP is $AM^{1-\alpha}$.

Conclusions

- ▶ Unified quantitative explanation for long-term changes in
 - ▶ Entry rate
 - ▶ Exit rates
 - ▶ Average firm size
 - ▶ Concentration
 - ▶ Labor Share
- ▶ Population growth as driving force
- ▶ Importance of firm demographics
- ▶ Interplay of population and firm demographics explains a large part of these facts



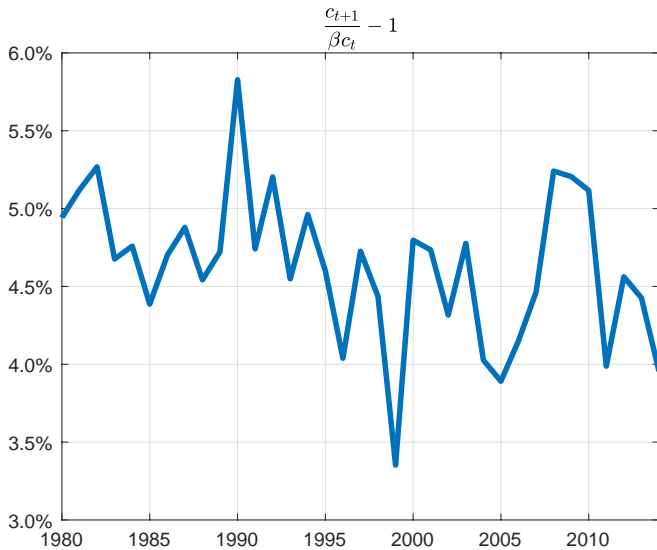
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Firm age

| | | | | |
|--------------|---------------|---------------|---------------|--------|
| — b) 1 | — c) 2 | — d) 3 | — e) 4 | — f) 5 |
| — g) 6 to 10 | — h) 11 to 15 | — i) 16 to 20 | — j) 21 to 25 | |

Implied interest rate with log utility

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Regression of reallocation rate on firm age

| Variable | Specification | | | |
|---------------------|----------------------|----------------------|----------------------|----------------------|
| | (1) | (2) | (3) | (4) |
| Year | -0.423*** (0.020) | -0.231*** (0.014) | -0.231*** (0.011) | -0.231*** (0.011) |
| AGE: | | | | |
| Age 1 | | 57.421*** (0.422) | 60.543*** (0.450) | 60.992*** (0.811) |
| Age 2 | | 47.321*** (0.429) | 50.443*** (0.455) | 52.719*** (0.823) |
| Age 3 | | 43.351*** (0.437) | 46.473*** (0.460) | 48.006*** (0.836) |
| Age 4 | | 40.915*** (0.446) | 44.037*** (0.465) | 45.051*** (0.848) |
| Age 5 | | 38.974*** (0.454) | 42.097*** (0.470) | 42.327*** (0.862) |
| Age 6 to 10 | | 35.972*** (0.499) | 39.095*** (0.500) | 38.718*** (0.937) |
| Age 11 to 15 | | 32.761*** (0.540) | 35.883*** (0.528) | 33.679*** (1.013) |
| Age 16 to 20 | | 30.965*** (0.588) | 34.087*** (0.561) | 30.609*** (1.108) |
| Age 21 to 25 | | 30.030*** (0.646) | 33.153*** (0.602) | 29.323*** (1.236) |
| SECTOR CONTROLS | No | No | Yes | Yes |
| SECTOR×AGE CONTROLS | No | No | No | Yes |
| Observations | 2,817 | 2,367 | 2,367 | 2,367 |
| R ² | 0.141 | 0.975 | 0.983 | 0.985 |

*** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

Regression of job creation rate on firm age

| Variable | Specification | | | |
|---------------------|----------------------|----------------------|----------------------|----------------------|
| | (1) | (2) | (3) | (4) |
| Year | -0.221*** (0.012) | -0.117*** (0.010) | -0.117*** (0.009) | -0.117*** (0.009) |
| AGE: | | | | |
| Age 1 | | 31.795*** (0.303) | 33.409*** (0.351) | 33.507*** (0.644) |
| Age 2 | | 24.325*** (0.309) | 25.939*** (0.355) | 28.023*** (0.653) |
| Age 3 | | 22.323*** (0.315) | 23.936*** (0.359) | 24.811*** (0.663) |
| Age 4 | | 21.174*** (0.321) | 22.788*** (0.363) | 23.092*** (0.673) |
| Age 5 | | 20.206*** (0.327) | 21.820*** (0.367) | 21.702*** (0.683) |
| Age 6 to 10 | | 18.476*** (0.359) | 20.090*** (0.390) | 19.810*** (0.743) |
| Age 11 to 15 | | 16.853*** (0.389) | 18.467*** (0.412) | 17.117*** (0.803) |
| Age 16 to 20 | | 16.324*** (0.423) | 17.938*** (0.438) | 16.088*** (0.879) |
| Age 21 to 25 | | 15.908*** (0.465) | 17.522*** (0.470) | 15.116*** (0.980) |
| SECTOR CONTROLS | No | No | Yes | Yes |
| SECTOR×AGE CONTROLS | No | No | No | Yes |
| Observations | 2,817 | 2,367 | 2,367 | 2,367 |
| R ² | 0.105 | 0.954 | 0.964 | 0.967 |

*** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

Regression of job destruction rate on firm age

| Variable | Specification | | | |
|---------------------|----------------------|----------------------|----------------------|----------------------|
| | (1) | (2) | (3) | (4) |
| Year | -0.259*** (0.014) | -0.125*** (0.011) | -0.125*** (0.010) | -0.125*** (0.010) |
| AGE: | | | | |
| Age 1 | | 34.426*** (0.354) | 35.072*** (0.399) | 36.933*** (0.743) |
| Age 2 | | 31.192*** (0.361) | 31.838*** (0.403) | 32.027*** (0.753) |
| Age 3 | | 27.792*** (0.367) | 28.439*** (0.408) | 29.024*** (0.765) |
| Age 4 | | 25.842*** (0.374) | 26.488*** (0.413) | 25.858*** (0.776) |
| Age 5 | | 24.119*** (0.381) | 24.766*** (0.417) | 24.353*** (0.789) |
| Age 6 to 10 | | 21.868*** (0.419) | 22.514*** (0.444) | 21.879*** (0.858) |
| Age 11 to 15 | | 19.477*** (0.453) | 20.124*** (0.468) | 19.707*** (0.927) |
| Age 16 to 20 | | 17.825*** (0.493) | 18.472*** (0.498) | 17.317*** (1.014) |
| Age 21 to 25 | | 17.459*** (0.543) | 18.106*** (0.535) | 17.470*** (1.131) |
| SECTOR CONTROLS | No | No | Yes | Yes |
| SECTOR×AGE CONTROLS | No | No | No | Yes |
| Observations | 2,817 | 2,367 | 2,367 | 2,367 |
| R ² | 0.103 | 0.956 | 0.967 | 0.969 |

*** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

Regression of log average firm size on firm age

| Variable | Specification | | | |
|---------------------|---------------------|----------------------|----------------------|----------------------|
| | (1) | (2) | (3) | (4) |
| Year | 0.006*** (0.001) | -0.005*** (0.001) | -0.005*** (0.000) | -0.005*** (0.000) |
| AGE: | | | | |
| Age 0 | | 1.839*** (0.023) | 1.435*** (0.015) | 1.441*** (0.026) |
| Age 1 | | 2.080*** (0.023) | 1.676*** (0.015) | 1.717*** (0.026) |
| Age 2 | | 2.171*** (0.023) | 1.767*** (0.015) | 1.806*** (0.026) |
| Age 3 | | 2.247*** (0.024) | 1.843*** (0.015) | 1.868*** (0.026) |
| Age 4 | | 2.319*** (0.024) | 1.915*** (0.015) | 1.941*** (0.026) |
| Age 5 | | 2.378*** (0.024) | 1.974*** (0.015) | 2.002*** (0.027) |
| Age 6 to 10 | | 2.526*** (0.027) | 2.122*** (0.016) | 2.159*** (0.029) |
| Age 11 to 15 | | 2.748*** (0.029) | 2.344*** (0.017) | 2.323*** (0.032) |
| Age 16 to 20 | | 2.977*** (0.032) | 2.573*** (0.018) | 2.472*** (0.035) |
| Age 21 to 25 | | 3.251*** (0.035) | 2.847*** (0.019) | 2.579*** (0.039) |
| SECTOR CONTROLS | No | No | Yes | Yes |
| SECTOR×AGE CONTROLS | No | No | No | Yes |
| R ² | 0.015 | 0.978 | 0.995 | 0.996 |
| Observations | 2,682 | 2,682 | 2,682 | 2,682 |

*** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

Regression of exit rate on firm age

| Variable | Specification | | | |
|---------------------|----------------------|----------------------|----------------------|----------------------|
| | (1) | (2) | (3) | (4) |
| Year | -0.151*** (0.012) | -0.011* (0.006) | -0.011** (0.005) | -0.011** (0.005) |
| AGE: | | | | |
| Age 1 | | 21.780*** (0.178) | 19.381*** (0.188) | 19.036*** (0.342) |
| Age 2 | | 16.143*** (0.178) | 13.744*** (0.188) | 12.702*** (0.342) |
| Age 3 | | 13.673*** (0.181) | 11.274*** (0.190) | 10.765*** (0.347) |
| Age 4 | | 12.029*** (0.185) | 9.629*** (0.192) | 9.380*** (0.352) |
| Age 5 | | 10.753*** (0.189) | 8.354*** (0.194) | 8.331*** (0.358) |
| Age 6 to 10 | | 8.647*** (0.208) | 6.247*** (0.206) | 6.695*** (0.390) |
| Age 11 to 15 | | 6.711*** (0.225) | 4.312*** (0.218) | 5.160*** (0.421) |
| Age 16 to 20 | | 5.901*** (0.246) | 3.501*** (0.232) | 4.582*** (0.461) |
| Age 21 to 25 | | 5.416*** (0.271) | 3.017*** (0.250) | 4.420*** (0.514) |
| SECTOR CONTROLS | No | No | Yes | Yes |
| SECTOR×AGE CONTROLS | No | No | No | Yes |
| R ² | 0.065 | 0.962 | 0.976 | 0.978 |
| Observations | 2,358 | 2,358 | 2,358 | 2,358 |

*** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

Regression of concentration on firm age

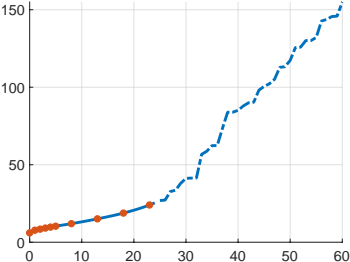
| Variable | Specification | |
|----------------|---------------------|--------------------|
| | (1) | (2) |
| Year | 0.003*** (0.001) | -0.000 (0.000) |
| AGE: | | |
| Age 0 | | 0.666 (0.439) |
| Age 1 | | 0.730* (0.439) |
| Age 2 | | 0.740* (0.440) |
| Age 3 | | 0.756* (0.440) |
| Age 4 | | 0.772* (0.440) |
| Age 5 | | 0.786* (0.440) |
| Age 6 to 10 | | 0.839* (0.440) |
| Age 11 to 15 | | 0.928** (0.441) |
| Age 16 to 20 | | 1.017** (0.441) |
| Age 21 to 25 | | 1.115** (0.442) |
| R ² | 0.080 | 0.976 |
| Observations | 301 | 301 |

*** $p < 0.01$; ** $p < 0.05$; * $p < 0.1$

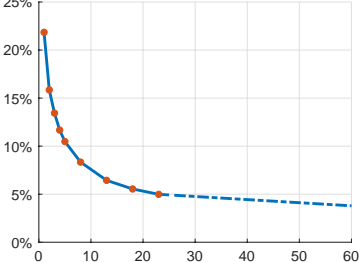
Extrapolation

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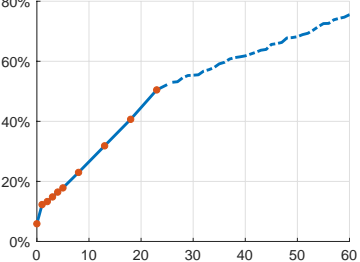
Firm size by age



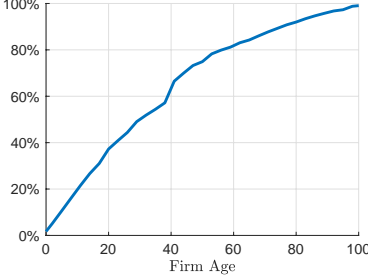
Firm exit rate by age



Firm concentration by age



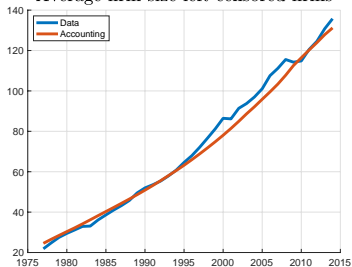
Employment Distribution in 1940



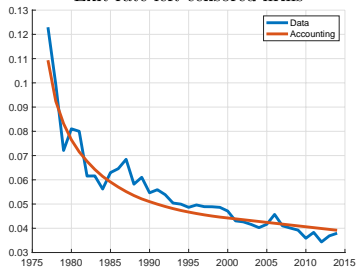
Accounting Exercise: Left-Censored Match

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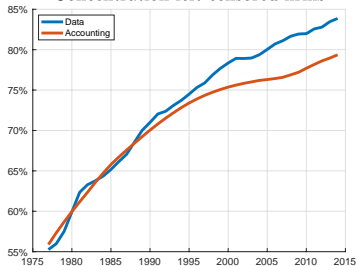
Average firm size left censored firms



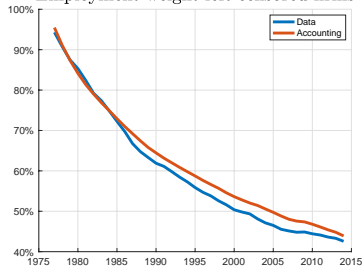
Exit rate left censored firms



Concentration left censored firms

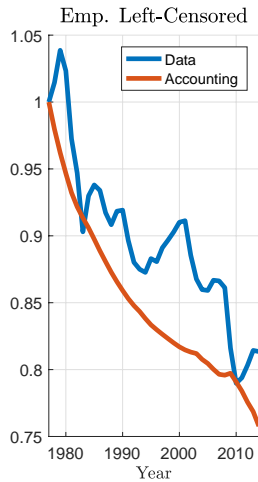
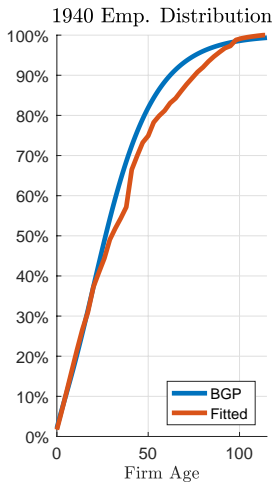
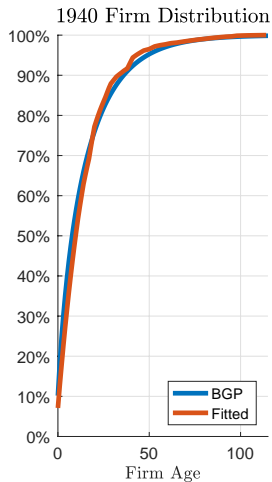


Employment weight left censored firms

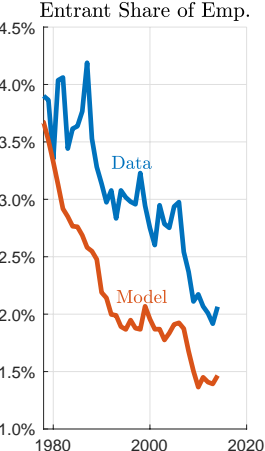
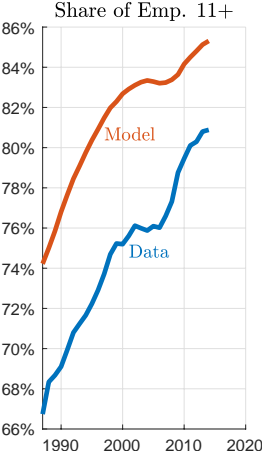
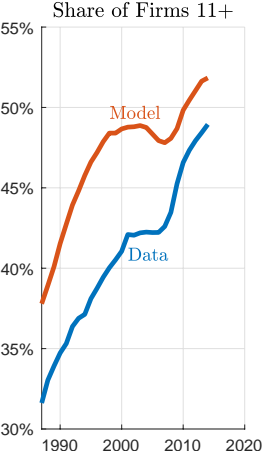


Accounting Exercise: Robustness checks

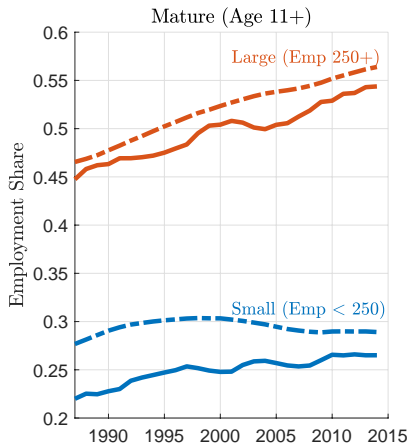
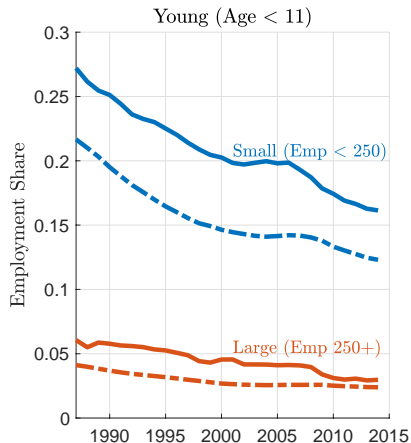
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Distributional Moments Match: Competitive Model

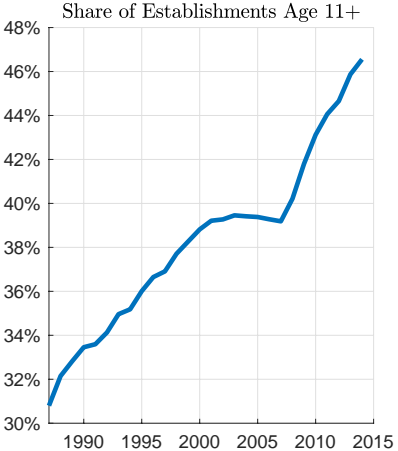


Age-Size Distribution Match: Competitive Model



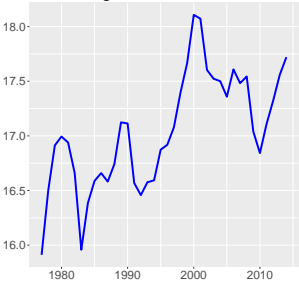
- ▶ Model: Dashed Line
- ▶ Data: Solid Line

Establishments

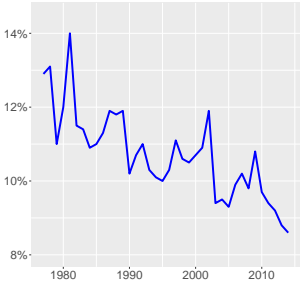


Establishments

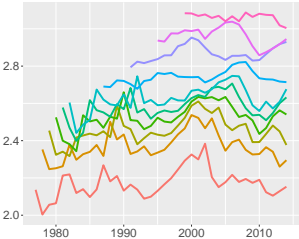
Average establishment size



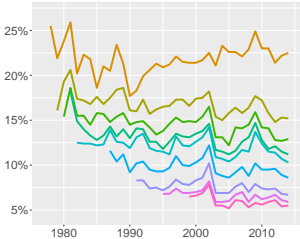
Exit rate



Log Avg. Estab. Size



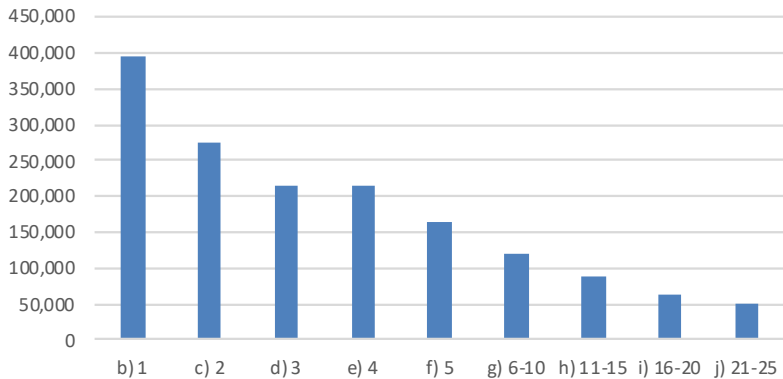
Exit Rate



Establishment age

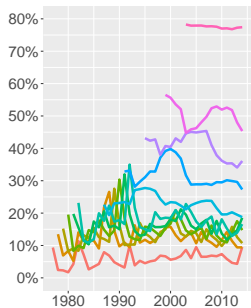
- a) 0
- b) 1
- c) 2
- d) 3
- e) 4
- f) 5
- g) 6 to 10
- h) 11 to 15
- i) 16 to 20
- j) 21 to 25

Employment Destroyed by Exit (adjusted per year)

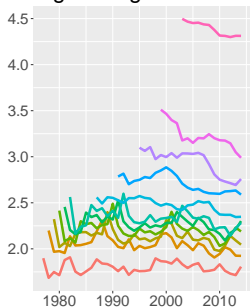


Statistics including firms age > 25

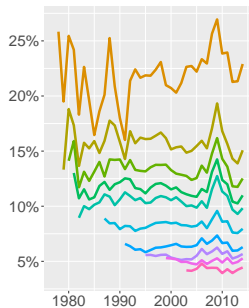
Concentration



Log Average Firm Size



Exit Rate



Firm age

| | | | | | |
|------------|-------------|-------------|-------------|-------------|------|
| a) 0 | b) 1 | c) 2 | d) 3 | e) 4 | f) 5 |
| g) 6 to 10 | h) 11 to 15 | i) 16 to 20 | j) 21 to 25 | k) Above 25 | |